## **Practice 1.2** (September 26)<sup>1</sup>

You have to fill this poll https://goo.gl/forms/CDXubqHnFvwBynnj1 before Monday 25, 10 pm.

- 1. Make a drawing in a square grid to make a representation of  $15 \times 12$ , and show how it can be used to compare the result with  $14 \times 13$ , without any calculation.
- 2. Compute  $45 \times 36$  using the ABN algorithm and the may an algorithm, and explain why the algorithms work.
- 3. Study whether  $a \times b$  is even or odd, in terms of the parity of a and b. Try to use an argument that can be used in Primary school.
- 4. What is the units digit of the following powers (explain your reasoning):

a)  $31^{125}$  b)  $42^{99}$  c)  $53^{219}$ 

- 5. Imagine that you have a weird calculator in which you can type only 2-digit numbers. Explain how you could compute the product  $8700036 \times 48$ .
- 6. If today is Tuesday 9 am, what time and what day of the week was it 20000 hours ago?
- 7. Find all 5-digit palindromic numbers in base 3 that are even numbers. (A number is palindromic if when read left to right is the same as when read right to left)
- 8. You have 1840 euros, and you have to give them to Alice y Bob, in the following ways:
  - a) First, in such a way that Alice gets 158 euros more than Bob.
  - b) Now, in such a way that Alice gets three times as much as Bob.

(Remember, problems must be solved without algebraic methods).

9. In the picture you can see an algorithm that computes  $927 \times 37$ . Analyze it and explain why it works.



10. Based on the consumption of last year, the administrator of a block of flats estimated that the gasoil that he had bought should be enough for 80 days. Nevertheless, the winter was mild, and daily consumption was 3 liters bigger than the forecast. If gasoil was over after 70 days, how many liters of gasoil did he bought at the beginning of the winter?

<sup>&</sup>lt;sup>1</sup>All problems should be made without using a calculator. In the future, problems meant to be solved with the help of a calculator will be marked with the symbol  $\bigcirc$ .